

## 2.4a Average Rate of Change

Estimate the velocity at  $t=3$  using the data

ave velocity =  $\Delta \text{distance} / \Delta \text{time}$   
 right hand difference quotient (rhdq)

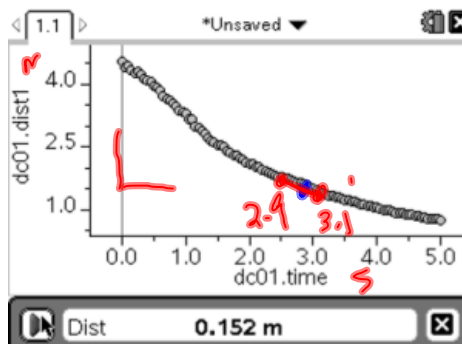
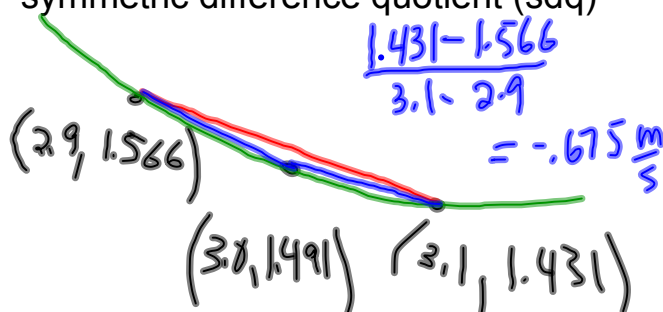
$$\frac{1.431 - 1.491}{3.1 - 3.0} = -0.6 \frac{\text{m}}{\text{s}}$$

left hand difference quotient (lhdq)

$$\frac{1.491 - 1.566}{3.0 - 2.9} = -0.75 \frac{\text{m}}{\text{s}}$$

symmetric difference quotient (sdq)

$$\frac{1.431 - 1.566}{3.1 - 2.9} = -0.675 \frac{\text{m}}{\text{s}}$$



Nick's walk  
 Nick walks quickly at first then slowly at the end  
 velocity changed

Aug 24-9:22 AM

Use a quadratic regression curve to estimate the velocity at  $t=3$

right hand difference quotient

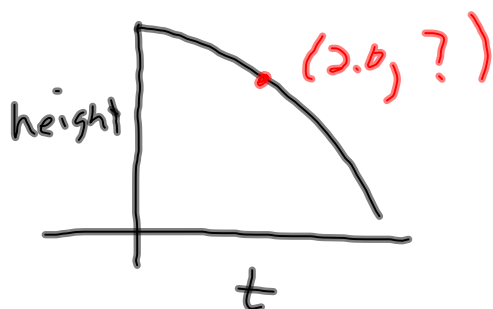
left hand difference quotient

symmetric difference quotient

↑  
 trace on the  
 graph of the  
 quadratic  
 equation

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A ball is dropped from the top of a 50 ft tower. Its height above ground after  $t$  seconds is  $50 - 16t^2$ . How fast is it falling after 2 seconds?



$$f_1(x) = 50 - 16x^2$$

sdg:

$$\frac{f_1(2.1) - f_1(1.9)}{2.1 - 1.9}$$

$$= -64 \frac{\text{ft}}{\text{sec}}$$

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The table shows the coordinates of a moving body. Estimate the velocity at  $t=2.5$ .

t sec	0	.5	1	1.5	2	2.5	3	3.5	4
s (ft)	3.5	-4	-8.5	-10	-8.5	-4	3.5	14	27.5

Use the data:

$$\frac{3.5 - -8.5}{3 - 2} = 12 \frac{\text{ft}}{\text{sec}}$$

Use a regression curve.

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